

## Estimates of anthropogenic carbon in the Indian Ocean with allowance for mixing and time-varying air-sea CO<sub>2</sub> disequilibrium

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[1] We apply to the Indian Ocean a novel technique to estimate the distribution, total mass, and net air-sea flux of anthropogenic carbon. Chlorofluorocarbon data are used to constrain distributions of transit times from the surface to the interior that are constructed to accommodate a range of mixing scenarios, from no mixing (pure bulk advection) to strong mixing. The transit time distributions are then used to propagate to the interior the surface water history of anthropogenic carbon estimated in a way that includes temporal variation in CO<sub>2</sub> air-sea disequilibrium. By allowing for mixing in transport and for variable air-sea disequilibrium, we remove two sources of positive bias common in other studies. We estimate that the anthropogenic carbon mass in the Indian Ocean was 14.3–20.5 Gt in 2000, and the net air-sea flux was 0.26–0.36 Gt/yr. The upper bound of this range, the no-mixing limit, generally coincides with previous studies, while the lower bound, the strong-mixing limit, is significantly below previous studies.

*INDEX TERMS:* 1635 Global Change: Oceans (4203); 4568 Oceanography: Physical: Turbulence, diffusion, and mixing processes; 4806 Oceanography: Biological and Chemical: Carbon cycling; 4808 Oceanography: Biological and Chemical: Chemical tracers; *KEYWORDS:* carbon, ocean, transport, mixing, age, Indian Ocean

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### 1. Introduction

[2] The ocean sequesters a large fraction of the CO<sub>2</sub> arising from human activity. While great progress has been made in estimating the distribution and mass of anthropogenic carbon in the ocean from observations, considerable uncertainty remains. The task is difficult because the anthropogenic signal of dissolved inorganic carbon ( $\Delta$ DIC) is of the order of 100 times smaller than natural DIC, which has complex, poorly known biochemical sources and sinks. Various  $\Delta$ DIC inference techniques have been developed [Brewer, 1978; Chen and Millero, 1979; Gruber *et al.*, 1996; Goyet *et al.*, 1999; Thomas and Ittekkot, 2001; McNeil *et al.*, 2003], and while comparison among them shows qualitative agreement, there are considerable quanti-

tative differences [Wanninkhof *et al.*, 1999; Sabine and Feely, 2001; Coatanoan *et al.*, 2001].

[3] Several assumptions are common to most  $\Delta$ DIC inference techniques, raising the possibility of overall bias across the range of estimates. Chief among these are (1) the assumption that mixing is a negligible component of transport and (2) the assumption of “constant disequilibrium” that  $\Delta$ DIC in surface waters has kept pace with increasing atmospheric CO<sub>2</sub>. Both of these assumptions have been questioned, but the errors incurred by making them have remained unclear. A number of studies have demonstrated that eddy mixing along constant density surfaces (isopycnals) plays a major role in propagating tracers [e.g., Jenkins, 1988; Robbins *et al.*, 2000] and must be taken into account when interpreting tracer-derived timescales [e.g., Thiele and Sarmiento, 1990; Sonnerup, 2001; Waugh *et al.*, 2003]. Information on the mixing, however, has not generally been incorporated in the observation-based  $\Delta$ DIC estimates. In addition to the weak-mixing and constant disequilibrium assumptions, techniques that derive  $\Delta$ DIC from total DIC measurements account for biochemical sources and sinks of DIC by using stoichiometric (Redfield) ratios among carbon, oxygen, and alkalinity, whose uncertainty impacts the  $\Delta$ DIC estimates [Wanninkhof *et al.*, 1999].

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[4] In this study we apply to the Indian Ocean a technique that avoids these assumptions. As in other studies we exploit the fact that  $\Delta\text{DIC}$  is well approximated as a passive, inert tracer transported by a steady state circulation on surfaces of constant density (isopycnals) in response to anthropogenic forcing in surface waters. Unlike other studies we relate interior  $\Delta\text{DIC}$  to the  $\Delta\text{DIC}$  history at the surface in a way that explicitly allows for mixing. CFC-12 data are used to constrain distributions of transit times from the surface to the interior that are designed to accommodate any proportion of diffusive mixing and bulk advection. The transit time distributions are then used to propagate to the interior the surface history of  $\Delta\text{DIC}$  estimated in a manner that allows for time-varying  $\text{CO}_2$  disequilibrium. The assumptions of no mixing and constant disequilibrium both lead to positive bias. By removing them, we obtain a range of values for Indian Ocean mass and net air-sea flux of anthropogenic carbon, all of which are consistent with the CFC data. The upper limit of the range approximately coincides with previous studies, while the lower limit is roughly one third lower.

## 2. Methodology

[5] We exploit the approximation, also made in other studies, that  $\Delta\text{DIC}$  penetrates the ocean as a passive, inert tracer. This is reasonable because, while the distribution of DIC itself is controlled by biology, upper ocean productivity is limited by nutrients, not carbon, and thus to first order the addition of anthropogenic carbon does not alter the rate of biological uptake and downward transport of carbon. Furthermore, as in other studies we assume the ocean circulation to be in steady state. *McNeil et al.* [2003] estimated from model studies that present-day secular change in the ocean circulation due to global warming alters carbon uptake by only 1%. Decadal and shorter time variability in the interior ocean does not affect our analysis significantly because many decades of tracer signal are integrated [*Hall et al.*, 2002]. However, annual and interannual variability of the outcrops of isopycnals causes uncertainty in estimating the histories of surface waters of  $\Delta\text{DIC}$  and CFC-12 (see section 3.2).

[6] We make use of the following relationship, valid for any passive, inert tracer transported by a steady state circulation in response to a uniform time-dependent surface forcing:

$$c_V(t) = \iint_0^\infty c_S(t-t') \mathcal{G}_V(t') dt', \quad (1)$$

where  $c_S(t)$  is the tracer concentration assumed to be uniform on the surface region  $S$  and  $c_V$  is the concentration averaged over a volume  $V$  that includes  $S$ .  $\mathcal{G}_V(t)$  is the distribution of transit times since the water in  $V$  last made contact with  $S$ , where it was labeled by tracer [*Beining and Roether*, 1996; *Haine and Hall*, 2002]. The mean tracer concentration in the volume comprises all the past contributions on the surface, weighted by  $\mathcal{G}_V$ . The shape of  $\mathcal{G}_V(t)$ , determined by the nature of the transport, will be estimated in section 2.1 by CFC-12 observations and inversion of relationship (1).

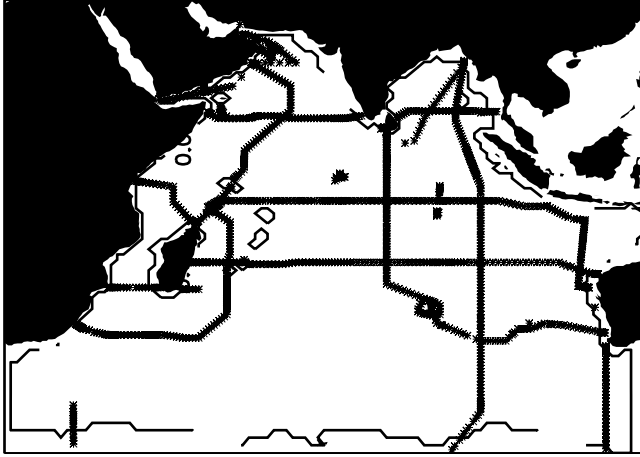
[7] While relationship (1) can be generalized to include spatially varying tracer concentration on the surface [*Haine and Hall*, 2002], uniform concentration on the surface is a good approximation in this application. The main thermocline of the Indian Ocean is ventilated predominantly from the south, through either winter subduction or mode water formation [*Karstensen and Quadfasel*, 2002], and anthropogenic tracers (or any air-sea flux anomaly) penetrate the upper ocean along isopycnals [*Fine et al.*, 1981]. Thus we can apply relationship (1) separately to northward transport along each isopycnal in response to time-varying tracer concentrations at the southern outcrop. Finally, because temperature is the most important factor determining both the solubilities of the tracers we consider and the density of seawater, tracer concentrations are approximately uniform along the outcrops.

[8] We neglect sources of water from the Red Sea. The volume flux from these sources is only 1–2% of the southern source [*Karstensen and Quadfasel*, 2002; *Bower et al.*, 2000], but because of the high temperature and salinity their fractional  $\Delta\text{DIC}$  contribution may be higher. (The solubility of DIC decreases with  $T$  and  $S$ , but  $\Delta\text{DIC}$  increases because of nonlinearities in DIC's dependence on  $T$ ,  $S$ , alkalinity, and atmospheric  $\text{CO}_2$ .) The error incurred by this neglect is estimated in section 3.2.

[9] Our analysis is performed separately on 15 isopycnals, the deepest of which ( $\sigma_\theta = 27.65$ ) reaches an approximate depth of 1500 m in southern midlatitudes. We find that the contribution to the total inventory decreases rapidly with density, with  $\sigma_\theta = 27.65$  containing less than 2% of the total  $\Delta\text{DIC}$  (compared with  $\sigma_\theta = 26.7$ , which contains 17% of the total). We assume that deeper isopycnals contribute insignificantly. North of 35 S the Indian Ocean is defined by its bounding land masses, while to the south it includes the sector of the Southern Ocean between 20 E and 120 E. The volumes  $V$  in expression (1), over which the tracer concentrations are averaged, are defined vertically by the separation of adjacent isopycnals, to the south by the outcrop regions (surfaces  $S$ ) of the isopycnals, and to the north by surfaces of constant concentration  $c$  of a specified tracer. A series of successively larger volumes is thereby defined as a function of  $c$ , the largest being the volume of the entire isopycnal slab. This formulation allows us to construct spatial distributions of  $\Delta\text{DIC}$  while at the same time enforcing certain global constraints (see section 2.1).

### 2.1. Constraining $\mathcal{G}_V(t)$

[10] To apply relationship (1) to  $\Delta\text{DIC}$ , we need  $\mathcal{G}_V(t)$  and  $\text{DIC}_S(t)$ , the history of  $\Delta\text{DIC}$  at the surface.  $\mathcal{G}_V(t)$  is obtained by inverting relationship (1) using observations of another passive, inert tracer, CFC-12, that has no natural background and a well-known atmospheric history. CFC-12 data from the World Ocean Circulation Experiment (WOCE) Indian Ocean cruise lines of 1994–1996 have been objectively mapped onto the isopycnal surfaces, and these 1° × 1° gridded data are used in our analysis. The surface outcrops are taken to be the intersection of the isopycnal with the surface. An example is shown in Figure 1. CFC-12 concentrations are largest at the southern outcrop and decrease to the north. The deepest isopycnals considered



**Figure 1.** CFC-12 concentration (pmol/L) on the  $\sigma_0 = 26.7$  isopycnal. The crosses indicate the locations of World Ocean Circulation Experiment (WOCE) CFC-12 measurements from which the distributions are formed.

have negligible CFC-12 through much of the northern Indian Ocean. To obtain the surface history at the outcrops,  $\text{CFC-12}_S(t)$ , we use the atmospheric history [Walker *et al.*, 2000] scaled to match the observed 1995 outcrop CFC-12 concentrations. In this way the degree of saturation at the outcrop is approximately included in  $\text{CFC-12}_S(t)$ . However, there is considerable uncertainty in  $\text{CFC-12}_S(t)$ , as the outcrop location and CFC-12 saturation vary seasonally and the observations are generally not taken at the time of subduction.

[11] We apply expression (1) to CFC-12 and invert parametrically for  $\mathcal{G}_V(t)$ . The following functional form of two parameters is assumed:

$$\mathcal{G}_V(t) = \frac{1}{\sqrt{\pi Pe \tau^2 t}} e^{-Pe t / 4\tau} e^{-Pe(\tau - t)^2 / 4\tau t} + \frac{1}{2\tau} \left[ \text{erf} \left( \sqrt{\frac{Pe t}{4\tau}} \right) + \text{erf} \left( \sqrt{\frac{Pe}{4\tau t}} (\tau - t) \right) \right] \quad (2)$$

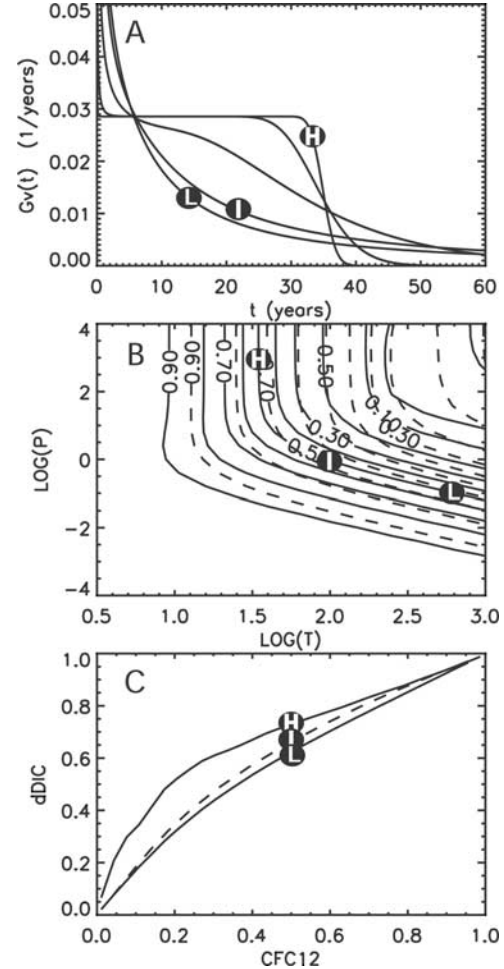
where  $\tau$  is a timescale equal to twice the mean transit time (“mean age”) of all the fluid elements in  $V$  and  $Pe = UL/\kappa$  is the Peclet number, given a characteristic velocity scale  $U$ , length scale  $L$ , and diffusivity  $\kappa$ . Large  $Pe$  corresponds to weak mixing. We discuss and illustrate this functional form in Appendix A.

[12] A range of transport scenarios, from no mixing and rapid bulk advection to strong mixing and slow bulk advection, is consistent with the CFC-12 observations, and thus CFC-12 can, at most, constrain  $\mathcal{G}_V(t)$  to a family of functions. Figure 2a shows examples of  $\mathcal{G}_V(t)$  at different parameter values, all of which produce the same volume-averaged concentration,  $\text{CFC-12}_V$ , when combined with  $\text{CFC-12}_S(t)$  via relationship (1). In the high- $Pe$  limit (no mixing), water and tracer march unmixed from the outcrop to the volume edge. All transit times less than  $\tau$ , the time to reach the volume edge, are represented with equal mass proportion, and no tracer is found at transit times greater

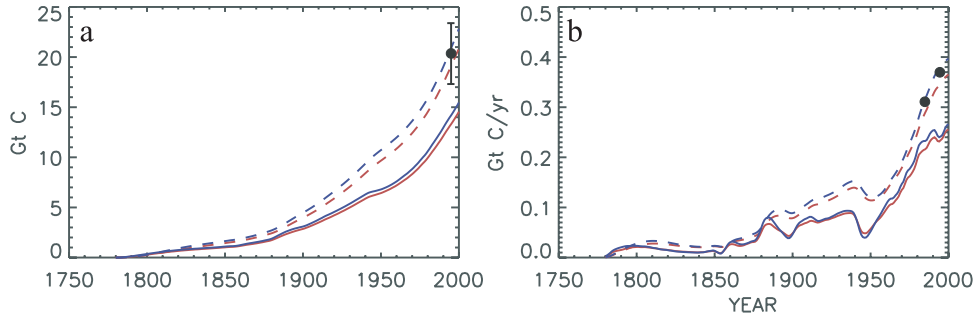
than  $\tau$ . In the low- $Pe$  limit (strong mixing),  $\mathcal{G}_V(t)$  heavily weights short transit times because of rapid recirculation with the surface but also has a long tail that extends well past  $\tau$  because of meandering pathways from the surface. An observation of  $\text{CFC-12}_V$  coupled with  $\text{CFC-12}_S(t)$ , constrains  $\tau$  and  $Pe$  to a locus of points (Figure 2b).

## 2.2. Applying $\mathcal{G}_V(t)$ to $\Delta\text{DIC}$

[13] To obtain  $\Delta\text{DIC}_S(t)$ , we begin with (but subsequently relax) the widely made constant disequilibrium assumption



**Figure 2.** (a) Examples of  $\mathcal{G}_V(t)$  that give rise to identical  $\text{CFC-12}_V$ . H is in the high  $Pe$  limit ( $Pe = 1000$  and  $\tau = 35$  years), I is intermediate ( $Pe = 1$  and  $\tau = 96$  years), and L is in the low  $Pe$  limit ( $Pe = 0.1$  and  $\tau = 630$  years). Two other  $\mathcal{G}_V(t)$  are shown between H and I ( $Pe = 100$ ,  $\tau = 35$  years and  $Pe = 10$ ,  $\tau = 40$  years). (b)  $\text{CFC-12}_V$  (solid curves) and  $\Delta\text{DIC}_V$  (dashed curves) versus  $\tau$  and  $Pe$  on log scales, expressed as fractions of their contemporary concentrations at the outcrop. The locations of the three  $\mathcal{G}_V(t)$  labeled in Figure 2a are shown. (c) Relationship between  $\text{CFC-12}_V$  and  $\Delta\text{DIC}_V$  from the contour intersections in Figure 2b, expressed as fractions of contemporary concentrations at the outcrop (solid curves). The  $\text{CFC-12}_V$ – $\Delta\text{DIC}_V$  relationship for  $Pe = 1$  (dashed curve) and the values corresponding to the three labeled  $\mathcal{G}_V(t)$  are shown.



**Figure 3.** (a) Total  $\Delta\text{DIC}$  mass in the Indian Ocean and (b) net air-sea flux into the Indian Ocean. Blue curves are derived from constant disequilibrium, and red curves are for time-varying disequilibrium. The dashed curves are the high  $Pe$  (no mixing) limit, and the solid curves are the low  $Pe$  (strong mixing) limit. In Figure 3a the circle with uncertainty bar ( $20.3 \pm 3$  Gt) is the estimate of *Sabine et al.* [1999]. In Figure 3b the circles are the estimates from *McNeil et al.* [2003] of net flux averaged over 1980–1989 (0.31 Gt C/yr) and 1990–1999 (0.37 Gt C/yr).

that anthropogenic  $\text{CO}_2$  in the atmosphere ( $\Delta\text{CO}_2(t)$ ) and  $\Delta\text{DIC}_S(t)$  evolve in lockstep, so that one may be obtained from the other using equilibrium carbon chemistry. In making the constant disequilibrium assumption, it is recognized that locally,  $\text{CO}_2$  across the air-sea interface is not in chemical equilibrium, but it is assumed that the degree of disequilibrium has not changed significantly since preindustrial times. Following *Thomas et al.* [2001], we form the difference time series  $\Delta\text{DIC}(t) = \text{DIC}(t) - \text{DIC}(1780)$ , where the year 1780 is selected as the start of the industrial era. (This definition is chosen for consistency with other studies. In 1780 ice core records indicate that atmospheric  $\text{CO}_2$  concentrations were about 280 ppm (E. M. Etheridge et al., Historical  $\text{CO}_2$  records from the Law Dome DE08, DE08-2, and DSS ice cores, in Trends: A Compendium of Data on Global Change, online database available at <http://cdiac.ornl.gov/trends/trends.htm>), which is the preindustrial level assumed by *Sabine et al.* [1999] and others. Estimates of instantaneous air-sea fluxes are not affected by the choice of preindustrial level.) The “disequilibrium term,” assumed to be constant, is present in both terms of the difference and thus cancels, leaving only the equilibrium terms. We can therefore solve the well-documented equilibrium inorganic chemistry system [e.g., *Lewis and Wallace*, 1988] to compute  $\Delta\text{DIC}_S(t)$ , given observations of temperature, salinity, alkalinity, and atmospheric  $\Delta\text{CO}_2(t)$ . In these calculations we use the carbonate dissociation coefficients of *Goyet and Poisson* [1989]. Use of other published coefficients makes a negligible difference in our estimates.

[14] The  $\Delta\text{DIC}_S(t)$  is convolved with  $\mathcal{G}_V(t)$  for a range of  $\tau$  and  $Pe$ , resulting in contours of volume-averaged concentration,  $\Delta\text{DIC}_V$  (Figure 2b). The intersection of  $\Delta\text{DIC}_V$  contours by a particular CFC-12 $_V$  contour is the constraint that the CFC-12 $_V$  observation imposes on  $\Delta\text{DIC}_V$ . Note that the chosen ranges of  $\tau$  and  $Pe$  are large enough that the CFC-12 $_V$  and  $\Delta\text{DIC}_V$  contours are parallel in the low and high limits. Any additional range of parameters results in no additional change in  $\Delta\text{DIC}_V$  for a given CFC-12 $_V$ . The minimum (strong mixing) to maximum (no mixing) range of  $\Delta\text{DIC}_V$  as a function of CFC-12 $_V$  obtained from the contour intersections is shown in Figure 2c. The tracer

concentrations are expressed as fractions of their contemporary outcrop values, which renders the CFC-12- $\Delta\text{DIC}$  relationship independent of the isopycnal.

[15] Because we assume steady state circulation,  $\mathcal{G}_V(t')$  in equation (1) depends on transit time  $t'$  but not on calendar date  $t$ . Therefore, once  $\mathcal{G}_V(t')$  is constrained, it can be applied to  $\Delta\text{DIC}$ , via equation (1), at any  $t$ . In this way, at each calendar year  $t$  we compute for each isopycnal  $\sigma$ , the mass  $\Delta M_{DIC}^\sigma = V_\sigma(\Delta\text{DIC}_V^\sigma)$ , where  $V_\sigma$  is the volume of the entire isopycnal slab. Summing over all isopycnals, we then have the history over the industrial era of anthropogenic carbon mass,  $\Delta M_{DIC}(t)$ , in the Indian Ocean, as well as the net air-sea flux,  $\Delta F_{DIC}(t) = d\Delta M_{DIC}/dt$ , into the Indian Ocean, at constant equilibrium (Figure 3).

### 2.3. Time-Varying $\text{CO}_2$ Disequilibrium

[16] The assumption of constant disequilibrium is erroneous. If the ocean were, on average, in equilibrium with the atmosphere in the preindustrial era but is now taking up some fraction of anthropogenic carbon, then the mean disequilibrium must have changed. It is the disequilibrium, the difference in  $\text{CO}_2$  across the air-sea interface, that drives the net air-sea flux. The anthropogenic component of the flux into isopycnal  $\sigma$  is

$$\Delta F_{DIC}^\sigma(t) = k[\Delta\text{CO}_2(t) - \alpha\Delta\text{DIC}_S(t)], \quad (3)$$

where  $\alpha$  is the equilibrium chemistry factor (dependent on temperature, salinity, and alkalinity) that converts  $\text{DIC}_S$  to the atmospheric  $\text{CO}_2$  with which it would be in equilibrium and  $k$  is the transfer coefficient, dependent on solubility and wind speed. If the disequilibrium has remained constant since the preindustrial era, then  $\Delta\text{CO}_2(t) - \alpha\Delta\text{DIC}_S(t) = 0$  and  $\Delta F_{DIC}^\sigma(t) = 0$ , inconsistent with the nonzero flux computed by assuming constant disequilibrium in the CFC-12 method (Figure 3).

[17] In order to resolve this inconsistency, we must modify  $\Delta\text{DIC}_S(t)$  and  $\Delta F_{DIC}(t)$  until they satisfy both equation (3) and our relationship between  $\Delta\text{DIC}_S(t)$  and  $\Delta F_{DIC}^\sigma(t)$  via the CFC-12-constrained  $\mathcal{G}_V(t)$ . That is, on each isopycnal  $\sigma$  we have two unknowns,  $\Delta\text{DIC}_S(t)$  and

$\Delta F_{DIC}^{\sigma}(t)$ , for which we solve simultaneously using expression (3) and

$$\Delta F_{DIC}^{\sigma}(t) = \frac{d}{dt} V_{\sigma} \int_0^{\infty} \Delta DIC_S(t-t') \mathcal{G}_V(t') dt', \quad (4)$$

the expression for the flux as the time rate of change of the mass obtained from  $\Delta DIC_S(t)$  via the CFC-12-constrained  $\mathcal{G}_V(t)$ . Equating equations (3) and (4) is the statement that the flux into the isopycnal slab must equal the mass rate of change within the slab and provides an integral equation for  $\Delta DIC_S(t)$ , which can be solved iteratively using the constant disequilibrium history as the first guess. Once  $\Delta DIC_S(t)$  is obtained,  $\Delta F_{DIC}^{\sigma}(t)$  can be computed from equation (4).

[18] In this solution we use values for the transfer coefficient  $k$  estimated by Carr *et al.* [2002], who employed the Wanninkhof [1992] wind speed parameterization and wind speeds from both Special Sensor Microwave Imager (SSM/I) and QuickSCAT scatterometer data. In addition, we require the areas  $A$  of the outcrop regions, which we take to equal the areas between surface CFC-12 contours at the southern extremities of adjacent isopycnals. Importantly, our mass and net air-sea flux estimates are relatively insensitive to the large uncertainty in  $k$  and  $A$  because the correction due to the relaxation of constant disequilibrium, shown in section 3, is small. For example,  $\pm 50\%$  uncertainty in  $k$  causes approximately  $\pm 5\%$  uncertainty in  $\Delta DIC$  mass and flux. The uncertainty in  $k$  impacts the magnitude of a first-order correction but not the zeroth-order estimate.

## 2.4. Computing Spatial Distributions

[19] In the calculation as described so far,  $V$  is equal to the entire volume of an isopycnal slab, from the southern outcrop to the northern continental boundary, and the resulting mass is the total anthropogenic carbon mass in the slab. However, to compute spatial  $\Delta DIC$  distributions, we estimate averaged concentrations  $\Delta DIC_V$  over a series of volumes  $V$  defined to the north by successively decreasing CFC-12 concentration contours. This formulation allows us to construct the spatial distributions while at the same time enforcing certain global constraints. If  $\Delta M_{DIC}^{\sigma}(V) = V(\Delta DIC_V)$  is the anthropogenic carbon mass in volume  $V$  of an isopycnal slab  $\sigma$  and  $\Delta M_{DIC}^{\sigma}(V + \delta V)$  is the mass in volume  $V + \delta V$ , then the mean concentration along the volume tube  $\delta V$  parallel to the CFC-12 contour is

$$\Delta DIC(V) = \frac{\Delta M_{DIC}^{\sigma}(V + \delta V) - \Delta M_{DIC}^{\sigma}(V)}{\delta V} = \frac{d\Delta M_{DIC}^{\sigma}(V)}{dV}. \quad (5)$$

We then transform from  $V$  coordinates to ‘‘CFC-12 equivalent latitude,’’ the latitude that encompasses the same volume as the CFC-12 contour defining  $V$ . Because CFC-12 contours are oriented approximately zonally, the CFC-12 equivalent latitude is similar to true latitude.

[20] In this manner we can form maps of the inferred  $\Delta DIC$  that approximate zonally averaged latitude-depth distributions. We can also plot the inferred  $\Delta DIC$  on each isopycnal versus longitude and latitude. Because we compute mean concentrations of  $\Delta DIC$  (minimum to maximum) on CFC contours, the resulting  $\Delta DIC$  contours on an

isopycnal are, by definition, parallel to the CFC-12 contours. Components of the  $\Delta DIC$  distribution perpendicular to CFC-12 are unavailable from CFC-12 data alone. However, contours of column  $\Delta DIC$ , formed from vertical integration over the isopycnals, are not necessarily parallel to contours of column CFC-12. The CFC-12 contour orientations vary with isopycnal, and the fractional contribution of an isopycnal to  $\Delta DIC$  column values is not generally the same as its fractional contribution to CFC-12 column values.

[21] The approach of estimating volume-averaged  $\Delta DIC$  is a modification of the technique described by Hall *et al.* [2002], who used tracer data to constrain the distributions of transit times  $\mathcal{G}(r, t)$  from the surface to particular locations  $r$ . We could follow that approach here to obtain point-wise estimates of  $\Delta DIC$  and then integrate spatially to arrive at total mass. However, such a procedure does not take advantage of a global constraint on  $\mathcal{G}_V(t)$  (the spatial integral of  $\mathcal{G}(r, t)$ ), namely, that  $\mathcal{G}_V(t)$  is a monotonically decreasing function of  $t$  when  $V$  represents the entire closed domain of the isopycnal slab. In the approach employed here, this constraint is enforced because the functional form for  $\mathcal{G}_V(t)$  is monotonically decreasing. Thus in cases such as the Indian Ocean where we have tracer data covering the entire domain, we use the approach developed here, while in cases where we analyze spatially limited data removed from the surface source, we use the Hall *et al.* [2002] approach.

## 3. Results

### 3.1. Inventory and Uptake

[22] We now apply this technique to compute the total mass, net air-sea flux, and spatial distribution of anthropogenic carbon in the Indian Ocean. To the degree the transport is in steady state, the constraint on  $\Delta DIC$  imposed by 1995 CFC-12 observations applies over the entire industrial era. We find that the mass of anthropogenic carbon and its net air-sea flux have risen nearly steadily in the industrial era (Figure 3). In the year 2000 we estimate that the  $\Delta DIC$  mass was 14.3–20.5 Gt and the net air-sea flux was 0.26–0.36 Gt/yr. The ranges are a result of the imperfect constraint CFC-12 imposes on  $\Delta DIC$  in the presence of mixing because of the tracers’ different histories. They do not represent statistical uncertainty, and no intermediate ‘‘best estimate’’ is available.

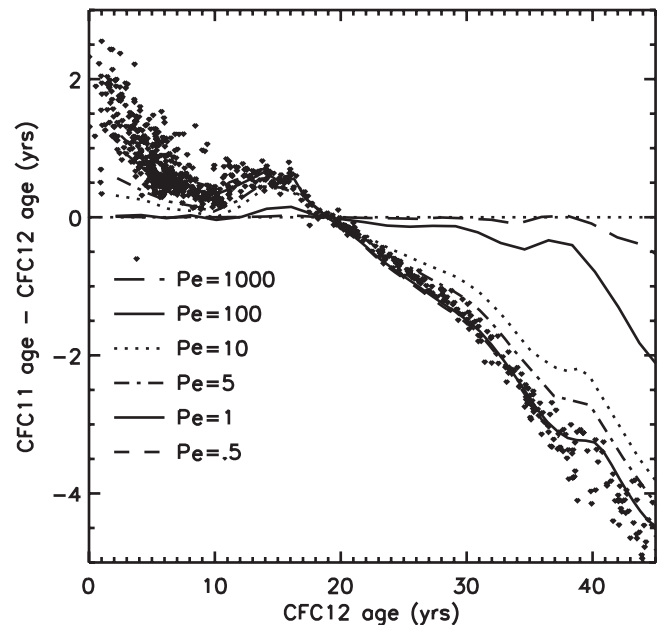
[23] Allowing for mixing significantly reduces the estimate of mass and net air-sea flux of anthropogenic carbon. For the Indian Ocean in 2000 the strong-mixing limit is lower than the no-mixing limit by 6.2 Gt in mass and 0.12 Gt/yr in net air-sea flux, reductions of 30% at constant disequilibrium. The effect of mixing can be understood by examining the analyses that have neglected it. Typically, a tracer ‘‘age’’ is defined as the time since the observed concentration of a tracer at an interior location was last exhibited at the surface. For example,  $CFC-12(t) = CFC-12_S(t - T_{CFC})$ , defining the CFC-12 age  $T_{CFC}$ . The tracer age is then applied to the surface history of anthropogenic carbon to estimate the concentration of  $\Delta DIC$  at the location:  $\Delta DIC(t) = \Delta DIC_S(t - T_{CFC})$ . In the absence of mixing this is valid because there is a unique transit time from the surface source region to the interior

location and the age of any tracer equals this transit time. In the presence of mixing, however, there is a wide distribution of transit times since water at the interior location was last at the surface and the tracer age is an average over the distribution, weighted by the tracer's history [Waugh *et al.*, 2003]. The age of a tracer such as CFC-12, whose history is shorter and more nonlinear than  $\Delta\text{DIC}$ , preferentially weights young components of the transit time distribution. The  $\Delta\text{DIC}$  surface history is evaluated at too recent a date, and the interior  $\Delta\text{DIC}$  concentration is overestimated. This bias is discussed in  $\Delta\text{DIC}$  studies using tracer ages [e.g., Gruber *et al.*, 1996], and its impact is examined in analyses of model data [Hall *et al.*, 2002; Matear *et al.*, 2003].

[24] The no-mixing values are upper bounds on the mass and net air-sea flux of anthropogenic carbon (Figure 3), but using CFC-12 alone, they are not ruled out. The simultaneous use of another tracer with a sufficiently distinct history imposes additional, independent constraints on  $\mathcal{G}_V(t)$  and narrows the range of  $\Delta\text{DIC}$  mass and net air-sea flux. Unfortunately, given uncertainties in the construction of inventories from sparse data, CFC-11 and CFC-12 are too similar to provide independent constraints on total  $\Delta\text{DIC}$  mass and net air-sea flux, while the peak in bomb tritium history is too broad and weak in the Southern Hemisphere for its attenuation to offer much additional constraint.

[25] However, if one restricts attention to diagnosing transport to locations of observation, rather than over the entire Indian Ocean domain, then formation of inventories is unnecessary and CFC-11 and CFC-12 data can be used constructively in combination [Waugh *et al.*, 2003]. Figure 4 shows a scatterplot of the difference of CFC-11 and CFC-12 concentration ages,  $\tau_{11} - \tau_{12}$ , versus the CFC-12 concentration age,  $\tau_{12}$ , for all data along the Indian Ocean WOCE line IO3, a longitudinal transect at 20 S. If transport from the surface to the points along the transect were purely bulk advective, then  $\tau_{11}$  would equal  $\tau_{12}$  everywhere and the observations in Figure 4 would fall along the zero line. This is clearly not the case. Mixing must play a role in the transport.

[26] To quantify the role of mixing, we follow Waugh *et al.* [2003] and use the two-parameter "inverse Gaussian" (IG) form for  $\mathcal{G}(t)$  (as opposed to  $\mathcal{G}_V(t)$ ) to model the IO3 CFC-11 and CFC-12 data. Surface time histories were constructed from the observed  $T$  and  $S$ , the solubility functions of Warner and Weiss [1985], and the atmospheric histories of Walker *et al.* [2000]. (In this case, rather than scaling the CFC histories by objectively mapped outcrop concentrations as was done for the inventory and uptake calculations, we simply assume the saturations to be 100%.) The surface histories are convolved with the IG  $\mathcal{G}(t)$ , whose parameters are selected such that the modeled  $\tau_{12}$  matches the observed  $\tau_{12}$  and  $Pe$  is constant along the transect. The curves in Figure 4 correspond to different assumed values of  $Pe$ . In the limit of high  $Pe$  (no mixing) the modeled CFC-11-CFC-12 relationship collapses to the zero line. By contrast, the curves for  $Pe = 10$  match the observed CFC-11-CFC-12 relationship in detail, with the best fits occurring for  $Pe = 1$ . (Curves with  $Pe = 1$  fall too close together to be

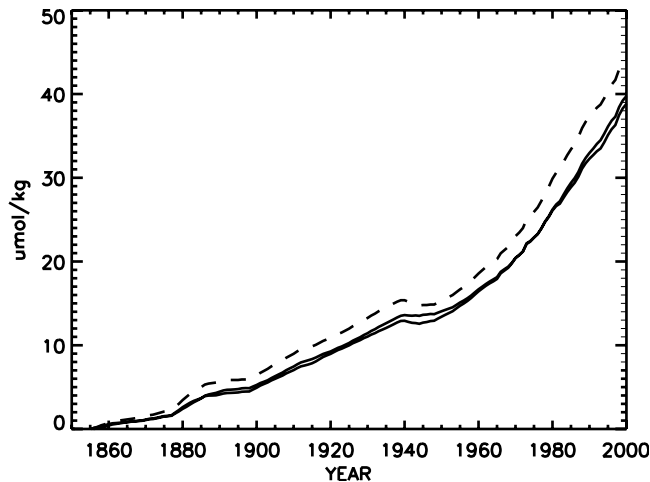


**Figure 4.** Difference of CFC-11 and CFC-12 concentration age plotted as a function of CFC-12 concentration age. The dots are from observations along WOCE transect IO3 (longitudinal transect at 20 S). The curves are fits to the data using the inverse Gaussian (IG) form for  $\mathcal{G}(t)$ , assuming different Peclet numbers,  $Pe$ , as listed in the key.

distinguished by the data.) Analysis of other WOCE Indian Ocean transects reveal similar behavior.

[27] Although we have not directly used CFC-11 and CFC-12 in combination to constrain  $\Delta\text{DIC}$  inventory and uptake, the behavior shown in Figure 4 strongly suggests that Indian Ocean transport is well outside the no-mixing, bulk advective limit. As shown in Figure 3c,  $Pe = 1$  places the domain mean  $\Delta\text{DIC}$  concentration in the lower half of the range determined from CFC-12 alone. This is in agreement with the analysis of CFCs and tritium in combination in the subpolar North Atlantic Ocean by Waugh *et al.* (D. W. Waugh *et al.*, Transport times and anthropogenic carbon in the subpolar North Atlantic Ocean, submitted to *Deep-Sea Research*, 2003, hereinafter referred to as Waugh *et al.*, submitted manuscript, 2003), who obtained transit time distributions in the strong-mixing limit and, consequently,  $\Delta\text{DIC}$  concentrations significantly lower than estimates from studies making the no-mixing assumption.

[28] Permitting variable disequilibrium further reduces the estimates of  $\Delta\text{DIC}$  mass and net air-sea flux.  $\Delta\text{DIC}$  is allowed to leave the mixed layer before equilibrating with new, higher atmospheric  $\text{CO}_2$  levels, and thus its surface history is reduced. The largest effect is found on the intermediate isopycnal,  $\sigma_\theta = 26.7$ , where  $\Delta\text{DIC}$  at the surface outcrop is reduced in 2000 by 10–12% (Figure 5). (When the disequilibrium is allowed to vary,  $\Delta\text{DIC}_S(t)$  itself becomes a function of transport. Pure bulk advection is more effective than mixing at pulling material away from the surface, so  $\Delta\text{DIC}_S(t)$  at high  $Pe$  is more reduced from constant disequilibrium, in this case 12% compared with



**Figure 5.** Time series of  $\Delta\text{DIC}$  surface concentration on the  $\sigma_0 = 26.6$  isopycnal assuming constant disequilibrium (dashed curve) and allowing time-varying disequilibrium in the no-mixing (lower solid curve) and strong-mixing (higher solid curve) limits.

10%.) The reduced surface history is transported to the interior, resulting in lower  $\Delta\text{DIC}$  mass. Providing for time-dependent disequilibrium reduces the estimate of Indian Ocean  $\Delta\text{DIC}$  mass in 2000 by 0.9 Gt for strong mixing and by 1.8 Gt for no mixing, fractional reductions of 5–10% compared with the no-mixing, constant disequilibrium result (Figure 3). The fractional reductions in net air-sea flux are similar.

### 3.2. Uncertainties

[29] There are several sources of uncertainty in our analysis. A first source comes from the objective mapping of CFC-12 from sparse cruise lines to gridded values on isopycnals. (CFC-12 measurement uncertainty itself is negligible.) This mapping introduces uncertainty in the CFC-12 isopycnal mean concentrations, which propagates nearly directly to uncertainty in inferred  $\Delta\text{DIC}$ . This can be seen simply by mapping an uncertainty range of  $\text{CFC-12}_V$  on the  $x$  axis of Figure 2c to a range of  $\Delta\text{DIC}_V$  on the  $y$  axis. The objective mapping routine applied to the CFC-12 data provides an uncertainty for the CFC-12 inventory on each isopycnal surface. These uncertainties varied from 7% to 16%, with a value of 14% for  $\sigma_0 = 26.7$ , the surface having the largest CFC-12 and  $\Delta\text{DIC}$  inventories.

[30] A second source of error comes from our neglect of Red Sea (RS) sources of tracer into the Indian Ocean thermocline. In order to put an upper bound on the  $\Delta\text{DIC}$  from these sources, we first note that *You and Tomczak* [1993] estimate 2% of the Indian Ocean thermocline to have RS origin. The fractional contribution to the  $\Delta\text{DIC}$  inventory may be higher because the  $\Delta\text{DIC}$  contribution increases with  $T$  and  $S$ . To estimate the maximum possible RS  $\Delta\text{DIC}$  contribution, we make the unrealistic assumption that RS water spreads instantaneously throughout the thermocline so that all RS water carries the most recent (and highest) possible  $\Delta\text{DIC}$  mole fraction. For  $T = 27$  and

$S = 40$  typical of the RS, this is  $\Delta\text{DIC}(2000) = 66 \mu\text{mol/kg}$ . Thus the upper bound on the RS contribution to the inventory is  $0.02 \cdot 66(V) = 0.9 \text{ Gt}$ , where  $V = 5.3 \cdot 10^7 \text{ km}^3$  is the Indian Ocean thermocline volume computed from the objectively mapped isopycnal depth fields. This mass represents 4–6% of our range on Indian Ocean  $\Delta\text{DIC}$  inventory.

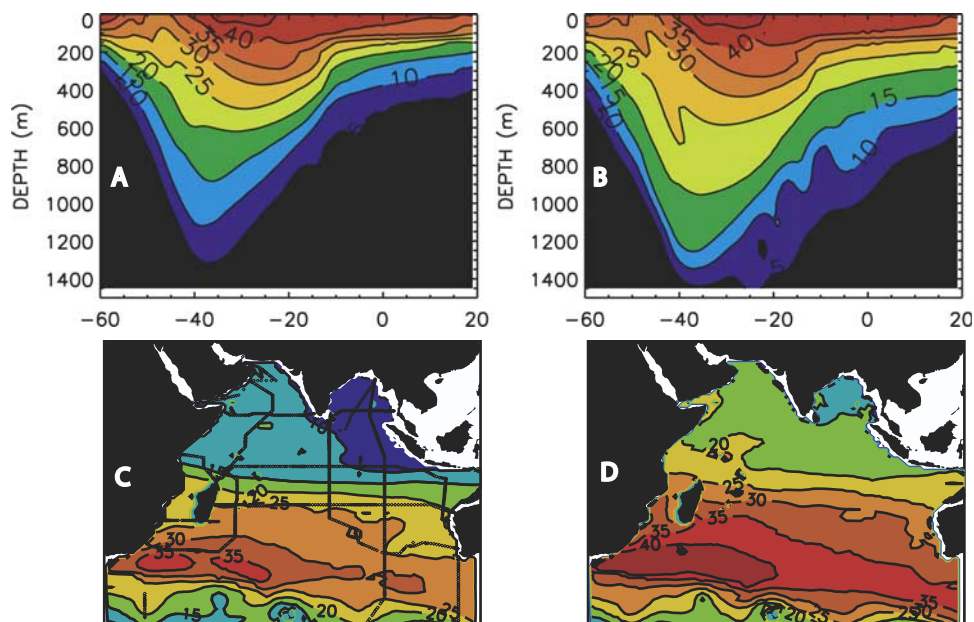
[31] In reality, the RS contribution will be significantly smaller than the 0.9 Gt upper bound. First, the RS source takes a finite time to propagate through the thermocline, so much of its water mass is aged and carries an older, lower  $\Delta\text{DIC}$  signal. Second, there is a partially compensating error due to the neglect of RS sources of CFC-12. We have assumed that the entire CFC-12 inventory originates in the south and have therefore overestimated the role of the southern CFC-12 source. This causes our estimate of the transit time distribution (TTD) from southern sources to be biased young, which in turn causes an overestimate of the southern  $\Delta\text{DIC}$  source. This overestimate is of the same order as the underestimate due to direct neglect of the RS  $\Delta\text{DIC}$  source, so there is a tendency for these errors to cancel.

[32] While the RS source is only a small contributor to the total Indian Ocean inventory, it is a significant contributor locally in the Arabian Sea. Therefore our neglect of an RS source causes our inferred  $\Delta\text{DIC}$  distributions in the Arabian Sea to be biased low, possibly by one third (a 5% total inventory error confined to 15% of the total volume).

[33] A third source of uncertainty arises from the imperfectly known CFC-12 histories at the southern outcrops. We have used the objectively mapped 1995 observations at the outcrops to scale the atmospheric CFC-12 history of *Walker et al.* [2000], which provides a boundary condition that implicitly includes CFC-12 disequilibrium. However, the objective mapping is least accurate in the Southern Ocean, where the observations are most scarce. Moreover, the measurements are not generally made during the season of subduction. To make a rough estimate of the impact on  $\Delta\text{DIC}$  of these uncertainties, we repeated the calculations using an equilibrium solubility calculation (100% saturation) for the CFC-12 outcrop histories, given the observed  $T$  and  $S$ . This results in a change to the 1995  $\Delta\text{DIC}$  inventory of 1.7 Gt, or 13% to 9% (strong-mixing to no-mixing limits).

[34] A fourth source of uncertainty arises from the selection of a particular functional form for the TTD. This uncertainty is very difficult to quantify. However, because the IG form used here can closely mimic TTDs simulated directly in numerical models (Appendix A), we think that its selection incurs an error that is small compared with other sources of uncertainty. In any case the IG form is a step beyond the assumption of no mixing that is implicit in previous studies that use tracer ages to lag  $\Delta\text{DIC}$  time series.

[35] Finally, all techniques to estimate anthropogenic carbon concentrations in the ocean assume that  $\Delta\text{DIC}$  propagates as a passive, inert tracer in a steady state circulation. This assumption causes error in  $\Delta\text{DIC}$  inference to the extent that ocean biota are evolving in response to increased carbon levels and ocean circulation is evolving in response to global



**Figure 6.** Ranges of the spatial distribution of  $\Delta$ DIC. (a) Minimum and (b) maximum  $\Delta$ DIC ( $\mu\text{mol/kg}$ ) versus equivalent latitude and depth. (c) Minimum and (d) maximum column  $\Delta$ DIC ( $\text{mol/m}^2$ ) versus longitude and latitude.

warming. At present, these effects are likely small compared with other uncertainties, but their importance will grow in the future [e.g., Sarmiento *et al.*, 1998].

### 3.3. Comparison With Other Estimates

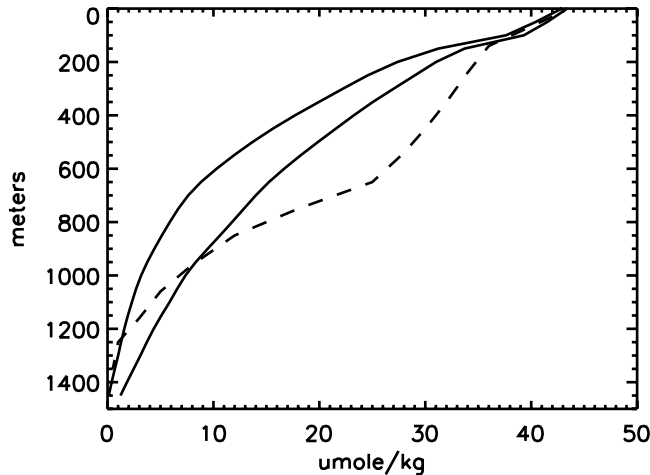
[36] The upper bounds of our estimated ranges of anthropogenic carbon mass in the Indian Ocean and its net air-sea flux just encompass those of other studies, while the lower bounds are significantly lower than other studies (Figure 3) because of the relaxation of the widely made assumptions of no mixing and constant disequilibrium, which cause positive bias. Sabine *et al.* [1999] estimated a 1995 mass of  $20.3 \pm 3$  Gt C, compared with our 13.1–18.8 Gt C. The central value of their range falls very close to our 1995 no-mixing, constant disequilibrium curve, consistent with expectation, as the Gruber *et al.* [1996] technique used by Sabine *et al.* [1999] makes these approximations. (Gruber *et al.* [1996] make the no-mixing assumption by using tracer ages to estimate disequilibrium terms, which are assumed to be constant. They reduce sensitivity to the no-mixing assumption by restricting application to waters with tracer ages less than a threshold.) McNeil *et al.* [2003], who also make these approximations by applying CFC-12 ages directly to  $\Delta$ DIC surface history, assuming constant disequilibrium, estimated a net air-sea flux into the Indian Ocean averaged over the interval 1980–1989 of 0.31 Gt C/yr and over the interval 1990–1999 of 0.37 Gt C/yr, compared with our ranges of 0.22–0.28 Gt C/yr and 0.24–0.34 Gt C/yr, respectively. Their estimates also fall on our constant disequilibrium, no-mixing curve.

[37] Our bounds on the spatial distribution of  $\Delta$ DIC concentration are shown in Figure 6.  $\Delta$ DIC penetrates most deeply in southern midlatitudes, the zone of subtropical

convergence, while below 800 m in the northern Indian Ocean, there is little  $\Delta$ DIC. This latitude-depth distribution is qualitatively similar to distributions of Sabine and Feely [2001], who compared the techniques of Gruber *et al.* [1996] and Chen and Millero [1979], although there are numerous differences in detail. Our latitude-longitude distribution of column inventories has an upper bound (no mixing) that peaks in southern midlatitudes at  $40 \text{ mol/m}^2$  and decreases to  $15 \text{ mol/m}^2$  in the Bay of Bengal. This is similar in shape to but slightly lower in magnitude than the column distribution estimated by Sabine and Feely [2001] using the Gruber *et al.* [1996] method. Our lower bound (strong mixing) is lower still, ranging from  $30 \text{ mol/m}^2$  to below  $10 \text{ mol/m}^2$ . The Sabine and Feely [2001] distribution using the Chen and Millero [1979] method has a significantly stronger latitudinal gradient, ranging from above  $55 \text{ mol/m}^2$  to below  $10 \text{ mol/m}^2$ .

[38] A comparison of the mean vertical  $\Delta$ DIC concentration profile estimated by Sabine *et al.* [1999] with our inferred range is shown in Figure 7. Sabine *et al.* [1999] used the inference method of Gruber *et al.* [1996]. In this method, on isopycnals that are believed to be everywhere contaminated by anthropogenic carbon, tracer ages (e.g., CFC ages) are used to estimate the  $\Delta$ DIC air-sea disequilibrium, which amounts to a neglect of mixing. The disequilibrium is overestimated, leading to an underestimate of the preindustrial background and, consequently, an overestimate of the anthropogenic component of total observed DIC (see Hall *et al.* [2002] for a more detailed discussion of this bias). In addition, the disequilibrium is assumed to be constant in time. Thus we expect the Sabine *et al.* [1999]  $\Delta$ DIC profile to exhibit a high bias in shallow regions. On the other hand, for deeper isopycnals that are believed to have regions old enough to be uncontaminated





**Figure 7.** Vertical profile of mean  $\Delta$ DIC concentration north of 35 S, minimum and maximum, as estimated in this study (solid curves). Also shown is a comparable profile estimated by *Sabine et al.* [1999] (dashed curve).

by  $\Delta$ DIC, *Gruber et al.* [1996] use measured DIC in these old regions as the preindustrial background to be subtracted from total DIC. If mixing brings small amounts of  $\Delta$ DIC into these old regions, then the preindustrial DIC is overestimated and  $\Delta$ DIC is underestimated. Thus we expect the *Sabine et al.* [1999] profile to be biased low in deeper waters.

[39] The *Sabine et al.* [1999] profile is, in fact, greater than our range above 950 m (except near the surface) and less than our range below 1200 m. While this behavior is generally consistent with expectation, the magnitude of the differences between 950 and 150 m cannot be explained solely by the no-mixing and constant disequilibrium biases. The no-mixing bias alone would put the *Sabine et al.* [1999] profile at most on our upper bound, and the constant disequilibrium bias is only a 5–10% effect (section 3.1). By contrast, at 600 m the *Sabine et al.* [1999]  $\Delta$ DIC concentration is 50% greater than our upper bound. We note that the *Gruber et al.* [1996] method makes use of Redfield ratios,  $R$ , in the construction of a quasi-conservative DIC tracer. *Wanninkhof et al.* [1999] have shown that realistic uncertainties in  $R$  can lead to large fractional errors at moderate  $\Delta$ DIC concentrations, which might explain some of the discrepancy. On the other hand, we have neglected  $\Delta$ DIC sources from the Red Sea. While this causes an underestimate in the total Indian Ocean inventory of less than 6% (section 3.2), the fractional error for the mean concentration north of 35° is somewhat higher.

#### 4. Summary

[40] We have developed and applied to the Indian Ocean a new technique to infer the distribution, inventory, and net air-sea flux of anthropogenic carbon. Observations of CFC-12 are used to constrain distributions of transit times from the surface to the interior that are designed to accommodate any proportion of diffusive mixing and bulk advection. The transit time distributions are then used to propagate into the

interior the surface water history of anthropogenic carbon estimated in a way that includes the natural temporal variation in  $\text{CO}_2$  air-sea disequilibrium. By allowing for mixing in transport and temporal variation in the air-sea  $\text{CO}_2$  disequilibrium, our technique removes two sources of positive bias found in most other studies.

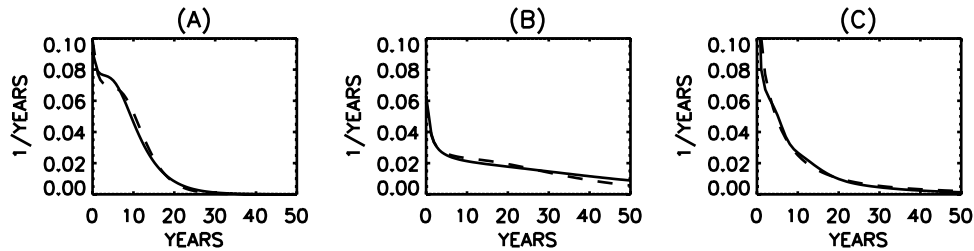
[41] We estimate that the anthropogenic carbon mass in the Indian Ocean was 14.3–20.5 Gt in 2000 and the net air-sea flux was 0.26–0.36 Gt/yr, with the low and high ends of the ranges representing strong-mixing and no-mixing transport limits. The ranges reflect the imperfect constraint that CFC-12 imposes on anthropogenic carbon because of the tracers' different histories. Our no-mixing estimates for the total mass and net air-sea flux of anthropogenic carbon in the Indian Ocean are in approximate agreement with other studies [*Sabine et al.*, 1999; *McNeil et al.*, 2003], while our strong-mixing estimates are significantly lower. Preliminary analysis of CFC-11 and CFC-12 in combination suggests that Indian Ocean transport is well outside the no-mixing limit and, consequently, that  $\Delta$ DIC inventory and uptake are in the lower half of its range, in agreement with a similar analysis in the subpolar North Atlantic (*Waugh et al.*, submitted manuscript, 2003).

[42] We have analyzed the Indian Ocean, whose contribution to the global ocean uptake of anthropogenic carbon is of the order of 20% [*Takahashi et al.*, 2002; *McNeil et al.*, 2003]. The biases shown here to be incurred in the Indian Ocean by the widely made assumptions of no mixing and constant disequilibrium are also relevant to other oceans. If the relaxation of these assumptions in other oceans leads to similar downward expansion in the estimated range of  $\Delta$ DIC, then the lower bounds on estimated  $\Delta$ DIC mass in the global ocean would have to be reduced by about a third. Even the upper bound of our uptake range, which agrees roughly with *McNeil et al.* [2003], is below the uptake predicted by many general circulation models [*McNeil et al.*, 2003; *Orr et al.*, 2001]. Uptake values at the lower end of our range would further exacerbate the discrepancy with these models.

#### Appendix A: Functional Form for Transit-Time Distribution

[43] Here we motivate and describe the two-parameter functional form used for the travel time distribution. Every parcel of water has a TTD since it was last at the surface. In the case of pure bulk advection the TTD is a narrow spike at a single transit time, the advective timescale. More generally, the TTD is broadly distributed because of mixing.

[44] A useful functional form for the TTD is the two-parameter inverse Gaussian (IG) form used, for example, by *Hall et al.* [2002] and *Waugh et al.* [2003]. The IG form is the boundary propagator solution to a semi-infinite one-dimensional advection-diffusion equation with constant coefficients. That is, it is the solution with no interior sources and a boundary condition of  $\mathcal{G}(t) = \delta(t)$ , where  $\delta(t)$  is the Dirac delta function. The IG form, however, has utility beyond idealized one-dimensional models and is a common statistical tool in the analysis of right-skewed data [*Seshadri*, 1999]. TTDs simulated directly in ocean general



**Figure A1.** Volume-transit time distributions (TTDs) as computed in three models: (a) Stommel gyre with a fast circulation ( $\tau = 15$  years and  $Pe = 16$ ), (b) Stommel gyre with a slow circulation ( $\tau = 48$  and  $Pe = 7.6$ ), and (c) subtropical mode water in a North Atlantic isopycnal general circulation model ( $\tau = 22$  years and  $Pe = 1.7$ ). In each case the dashed curves are the best fits using the IG volume-TTD form.

circulation models generally have early peaks, representing advective transport along some dominant pathway, and long tails, due to along flow and lateral mixing [e.g., *Khaliwala et al.*, 2001; *Haine and Hall*, 2002; F. Primeau, Characterizing transport between the surface mixed layer and the ocean interior with a forward and adjoint global ocean transport model, submitted to *Journal of Physical Oceanography*, 2003]. While the circulation is complex and two- or three-dimensional, the TTD can often (but not always) be well fit by the IG form.

[45] In this study we want to parameterize the TTD averaged over a volume that includes, as one boundary, the surface source region. That is, we want to parameterize

$$\mathcal{G}_V(t) = \frac{1}{V} \int_V d^3r \mathcal{G}(r, t). \quad (\text{A1})$$

$\mathcal{G}(t)$  is the distribution of transit times since water in the volume  $V$  (one boundary of which is the surface source region) made last contact with the surface source region. The IG form for  $\mathcal{G}_V(t)$  is obtained by averaging the IG form over a one-dimensional “volume” extending from the origin to some position whose value is expressed in terms of mean transit time. One obtains functional form (2), whose parameters are  $\tau$ , twice the mean transit time (“mean age”) of all the fluid elements in  $V$ , and  $Pe$ , the Peclet number, defined as the ratio of diffusive to advective timescales.

[46] While the volume-TTD of real ocean domains may differ considerably in detail from the IG form, there are certain general properties of volume-TTD that the IG form captures: (1) For a closed domain,  $\mathcal{G}_V(t)$  is a nonincreasing function of  $t$  [*Haine and Hall*, 2002], simply the statement that every parcel at transit time (“age”)  $t$  must have passed through every earlier transit time. (2)  $\mathcal{G}_V(t)$  is singular at  $t = 0$  [*Holzer and Hall*, 2000]. (3) The large  $t$  limit of  $\mathcal{G}_V(t)$  is exponential decay [*Haine and Hall*, 2002].

[47] To illustrate the utility of the volume-IG form, we have fit it to the  $\mathcal{G}_V$  simulated directly in a two-dimensional Stommel gyre model and a general circulation model (GCM). The Stommel gyre model is configured as by *Thiele and Sarmiento* [1990]. Figures A1a and A1b show  $\mathcal{G}_V(t)$  for the whole two-dimensional model domain in two sample circulations, fast and slow. Also shown are best fit IG forms, which have the parameters  $\tau = 15$  years and  $Pe = 16$  for the fast circulation and  $\tau = 48$  years and  $Pe = 7.6$  for the slow

circulation. Figure A1c shows the  $\mathcal{G}_V(t)$  for subtropical mode water in the North Atlantic as simulated by *Haine and Hall* [2002] using an isopycnal GCM. (The  $\mathcal{G}_V(t)$  of Figure A2c is equivalent to that shown in Figure 8d of Haine and Hall but plotted on a linear scale.) The best fit IG has the parameters  $\tau = 22$  years and  $Pe = 1.7$ . In all three cases the IG form closely mimics the directly simulated TTD, giving us confidence in its application to observational data.

[48] **Acknowledgments.** We thank M. Follows for his equilibrium inorganic carbon system code, Bill Smethie for discussions on CFC inventory uncertainties, and Chris Sabine and an anonymous reviewer for comments that led to an improved manuscript. This work was supported in part by a grant from the National Science Foundation OCE physical oceanography program.

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